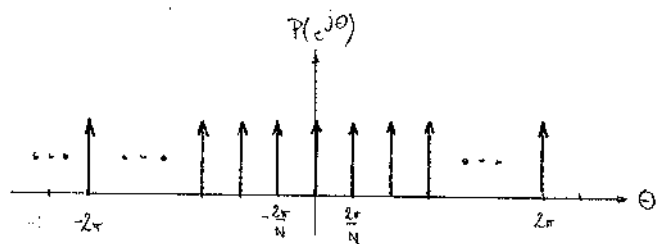


$$(a) \quad p[n] = \sum_{k=-\infty}^{\infty} \delta[n-kN] \quad \rightarrow \quad P(e^{j\theta}) = \frac{1}{N} \sum_{k=-\infty}^{\infty} \delta\left(\theta - \frac{2\pi}{N}k\right) = \frac{1}{N} \delta_{\frac{2\pi}{N}}(\theta)$$

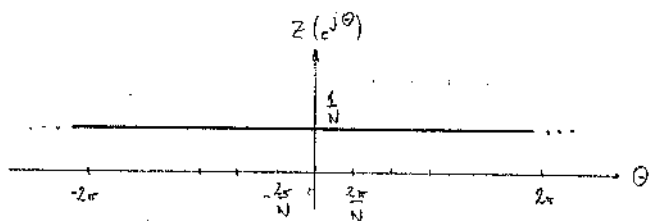


$$z[n] = x[n] \cdot p[n]$$

$$X(e^{j\theta}) = \text{rect}_{2\pi}\left(\frac{\theta}{2\pi}\right) \rightarrow x[n] = \frac{\sin\left(\frac{\pi}{N}n\right)}{\pi n}$$

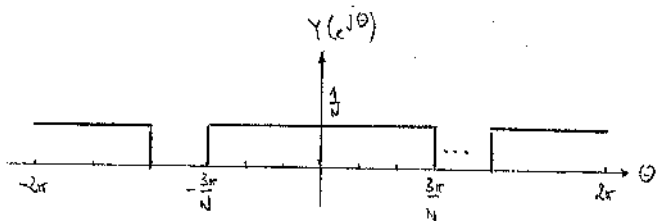
$$z[n] = \sum_{k=-\infty}^{\infty} \delta[n-kN] \cdot \frac{\sin\left(\frac{\pi}{N}n\right)}{\pi n} = \delta[n] \frac{\sin\left(\frac{\pi}{N}n\right)}{\pi n} = \frac{1}{N} \delta[n]$$

$$Z(e^{j\theta}) = \frac{1}{N}$$



$$y[n] = (z * h_{rp})[n] \rightarrow Z(e^{j\theta}) \cdot H_{rp}(e^{j\theta}) = Y(e^{j\theta})$$

$$Y(e^{j\theta}) = \frac{1}{N} \text{rect}_{2\pi}\left(\frac{\theta}{\frac{6\pi}{N}}\right)$$



$$(b) \quad y[n] = \frac{1}{N} \frac{\sin\left(\frac{3\pi}{N}n\right)}{\pi n}$$